

## CHAPTER 17

# Diffraction and Interference



**Figure 17.1** The colors reflected by this compact disc vary with angle and are not caused by pigments. Colors such as these are direct evidence of the wave character of light. (credit: Reggie Mathalone)

### Chapter Outline

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#### [17.1 Understanding Diffraction and Interference](#)

#### [17.2 Applications of Diffraction, Interference, and Coherence](#)

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**INTRODUCTION** Examine a compact disc under white light, noting the colors observed and their locations on the disc. Using the CD, explore the spectra of a few light sources, such as a candle flame, an incandescent bulb, and fluorescent light. If you have ever looked at the reds, blues, and greens in a sunlit soap bubble and wondered how straw-colored soapy water could produce them, you have hit upon one of the many phenomena that can only be explained by the wave character of light. That and other interesting phenomena, such as the dispersion of white light into a rainbow of colors when passed through a narrow slit, cannot be explained fully by geometric optics. In such cases, light interacts with small objects and exhibits its wave characteristics. The topic of this chapter is the branch of optics that considers the behavior of light when it exhibits wave characteristics.

## 17.1 Understanding Diffraction and Interference

### Section Learning Objectives

*By the end of this section, you will be able to do the following:*

- Explain wave behavior of light, including diffraction and interference, including the role of constructive and destructive interference in Young's single-slit and double-slit experiments
- Perform calculations involving diffraction and interference, in particular the wavelength of light using data from a two-slit interference pattern

### Section Key Terms

diffraction    Huygens's principle    monochromatic    wavefront

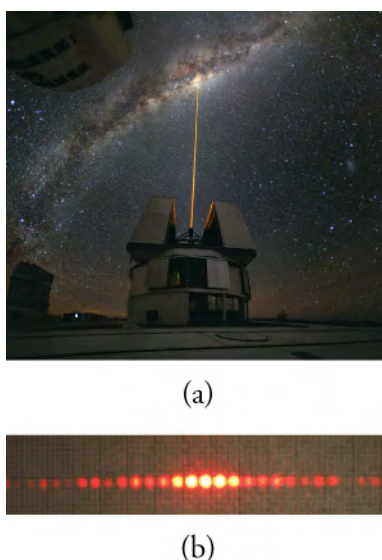
## Diffraction and Interference

We know that visible light is the type of electromagnetic wave to which our eyes responds. As we have seen previously, light obeys the equation

$$c = f\lambda,$$

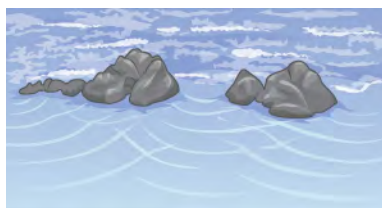
where  $c = 3.00 \times 10^8$  m/s is the speed of light in vacuum,  $f$  is the frequency of the electromagnetic wave in Hz (or  $\text{s}^{-1}$ ), and  $\lambda$  is its wavelength in m. The range of visible wavelengths is approximately 380 to 750 nm. As is true for all waves, light travels in straight lines and acts like a ray when it interacts with objects several times as large as its wavelength. However, when it interacts with smaller objects, it displays its wave characteristics prominently. Interference is the identifying behavior of a wave.

In [Figure 17.2](#), both the ray and wave characteristics of light can be seen. The laser beam emitted by the observatory represents ray behavior, as it travels in a straight line. Passing a pure, one-wavelength beam through vertical slits with a width close to the wavelength of the beam reveals the wave character of light. Here we see the beam spreading out horizontally into a pattern of bright and dark regions that are caused by systematic constructive and destructive interference. As it is characteristic of wave behavior, interference is observed for water waves, sound waves, and light waves.



**Figure 17.2** (a) The light beam emitted by a laser at the Paranal Observatory (part of the European Southern Observatory in Chile) acts like a ray, traveling in a straight line. (credit: Yuri Beletsky, European Southern Observatory) (b) A laser beam passing through a grid of vertical slits produces an interference pattern—characteristic of a wave. (credit: Shim'on and Slava Rybka, Wikimedia Commons)

That interference is a characteristic of energy propagation by waves is demonstrated more convincingly by water waves. [Figure 17.3](#) shows water waves passing through gaps between some rocks. You can easily see that the gaps are similar in width to the wavelength of the waves and that this causes an interference pattern as the waves pass beyond the gaps. A cross-section across the waves in the foreground would show the crests and troughs characteristic of an interference pattern.



**Figure 17.3** Incoming waves (at the top of the picture) pass through the gaps in the rocks and create an interference pattern (in the foreground).

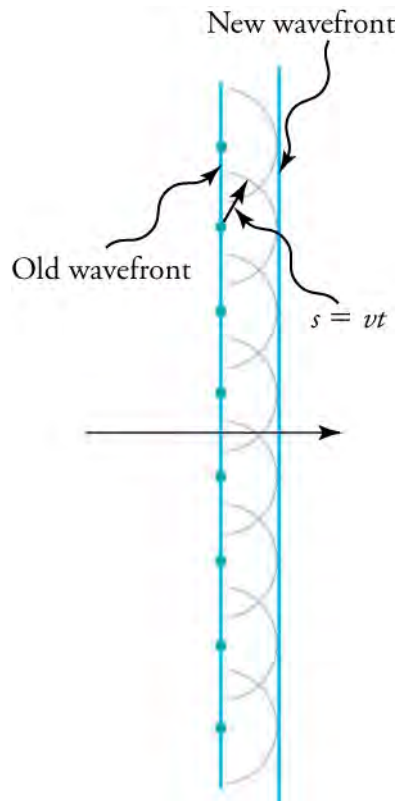
Light has wave characteristics in various media as well as in a vacuum. When light goes from a vacuum to some medium, such as water, its speed and wavelength change, but its frequency,  $f$ , remains the same. The speed of light in a medium is  $v = c/n$ , where  $n$  is its index of refraction. If you divide both sides of the equation  $c = f\lambda$  by  $n$ , you get  $c/n = v = f\lambda/n$ . Therefore,  $v = f\lambda_n$ , where  $\lambda_n$  is the wavelength in a medium, and

$$\lambda_n = \frac{\lambda}{n},$$

where  $\lambda$  is the wavelength in vacuum and  $n$  is the medium's index of refraction. It follows that the wavelength of light is smaller in any medium than it is in vacuum. In water, for example, which has  $n = 1.333$ , the range of visible wavelengths is  $(380 \text{ nm})/1.333$  to  $(760 \text{ nm})/1.333$ , or  $\lambda_n = 285\text{--}570 \text{ nm}$ . Although wavelengths change while traveling from one medium to another, colors do not, since colors are associated with frequency.

The Dutch scientist Christiaan Huygens (1629–1695) developed a useful technique for determining in detail how and where waves propagate. He used **wavefronts**, which are the points on a wave's surface that share the same, constant phase (such as all the points that make up the crest of a water wave). **Huygens's principle** states, “Every point on a wavefront is a source of wavelets that spread out in the forward direction at the same speed as the wave itself. The new wavefront is a line tangent to all of the wavelets.”

[Figure 17.4](#) shows how Huygens's principle is applied. A wavefront is the long edge that moves; for example, the crest or the trough. Each point on the wavefront emits a semicircular wave that moves at the propagation speed  $v$ . These are drawn later at a time,  $t$ , so that they have moved a distance  $s = vt$ . The new wavefront is a line tangent to the wavelets and is where the wave is located at time  $t$ . Huygens's principle works for all types of waves, including water waves, sound waves, and light waves. It will be useful not only in describing how light waves propagate, but also in how they interfere.

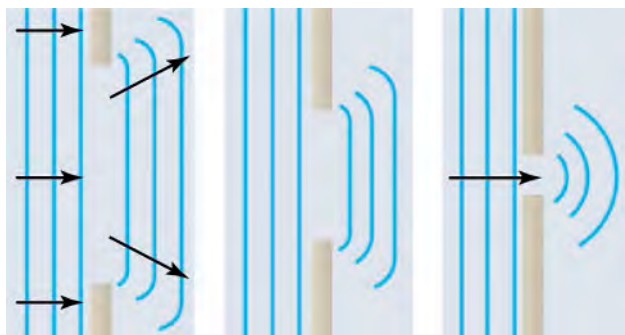


**Figure 17.4** Huygens's principle applied to a straight wavefront. Each point on the wavefront emits a semicircular wavelet that moves a distance  $s = vt$ . The new wavefront is a line tangent to the wavelets.

What happens when a wave passes through an opening, such as light shining through an open door into a dark room? For light, you expect to see a sharp shadow of the doorway on the floor of the room, and you expect no light to bend around corners into other parts of the room. When sound passes through a door, you hear it everywhere in the room and, thus, you understand that sound spreads out when passing through such an opening. What is the difference between the behavior of sound waves and light waves in this case? The answer is that the wavelengths that make up the light are very short, so that the light acts like a ray. Sound has wavelengths on the order of the size of the door, and so it bends around corners.

If light passes through smaller openings, often called slits, you can use Huygens's principle to show that light bends as sound does (see [Figure 17.5](#)). The bending of a wave around the edges of an opening or an obstacle is called **diffraction**. Diffraction is a

wave characteristic that occurs for all types of waves. If diffraction is observed for a phenomenon, it is evidence that the phenomenon is produced by waves. Thus, the horizontal diffraction of the laser beam after it passes through slits in [Figure 17.2](#) is evidence that light has the properties of a wave.



**Figure 17.5** Huygens's principle applied to a straight wavefront striking an opening. The edges of the wavefront bend after passing through the opening, a process called diffraction. The amount of bending is more extreme for a small opening, consistent with the fact that wave characteristics are most noticeable for interactions with objects about the same size as the wavelength.

Once again, water waves present a familiar example of a wave phenomenon that is easy to observe and understand, as shown in [Figure 17.6](#).



**Figure 17.6** Ocean waves pass through an opening in a reef, resulting in a diffraction pattern. Diffraction occurs because the opening is similar in width to the wavelength of the waves.



## WATCH PHYSICS

### Single-Slit Interference

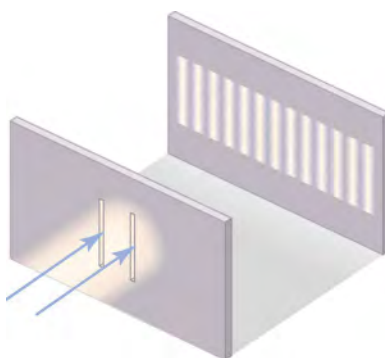
This video works through the math needed to predict diffraction patterns that are caused by single-slit interference.

[Click to view content \(https://www.openstax.org/l/28slit\)](https://www.openstax.org/l/28slit)

Which values of  $m$  denote the location of destructive interference in a single-slit diffraction pattern?

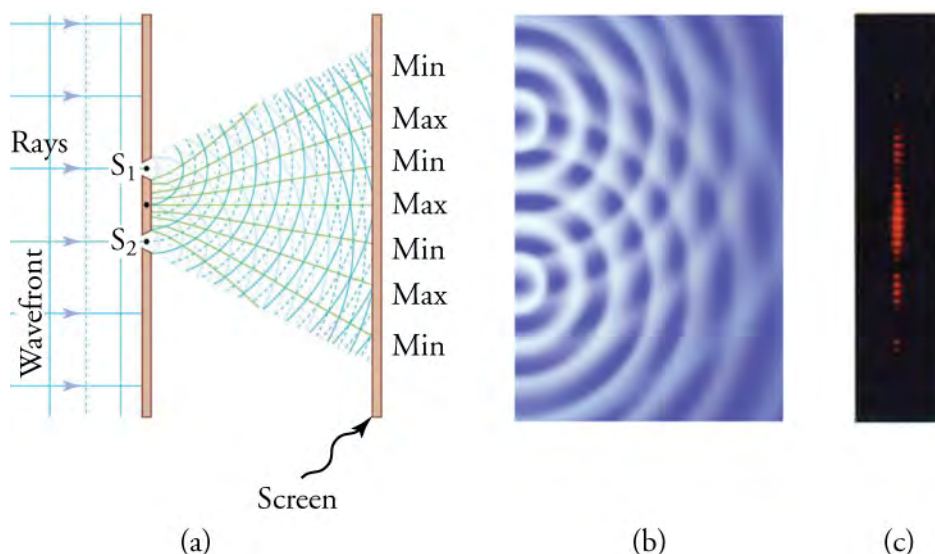
- whole integers, excluding zero
- whole integers
- real numbers excluding zero
- real numbers

The fact that Huygens's principle worked was not considered enough evidence to prove that light is a wave. People were also reluctant to accept light's wave nature because it contradicted the ideas of Isaac Newton, who was still held in high esteem. The acceptance of the wave character of light came after 1801, when the English physicist and physician Thomas Young (1773–1829) did his now-classic double-slit experiment (see [Figure 17.7](#)).



**Figure 17.7** Young's double-slit experiment. Here, light of a single wavelength passes through a pair of vertical slits and produces a diffraction pattern on the screen—numerous vertical light and dark lines that are spread out horizontally. Without diffraction and interference, the light would simply make two lines on the screen.

When light passes through narrow slits, it is diffracted into semicircular waves, as shown in [Figure 17.8](#) (a). Pure constructive interference occurs where the waves line up crest to crest or trough to trough. Pure destructive interference occurs where they line up crest to trough. The light must fall on a screen and be scattered into our eyes for the pattern to be visible. An analogous pattern for water waves is shown in [Figure 17.8](#) (b). Note that regions of constructive and destructive interference move out from the slits at well-defined angles to the original beam. Those angles depend on wavelength and the distance between the slits, as you will see below.



**Figure 17.8** Double slits produce two sources of waves that interfere. (a) Light spreads out (diffracts) from each slit, because the slits are narrow. The waves overlap and interfere constructively (bright lines) and destructively (dark regions). You can only see the effect if the light falls onto a screen and is scattered into your eyes. (b) The double-slit interference pattern for water waves is nearly identical to that for light. Wave action is greatest in regions of constructive interference and least in regions of destructive interference. (c) When light that has passed through double slits falls on a screen, we see a pattern such as this.

## Virtual Physics

### Wave Interference

[Click to view content \(https://www.openstax.org/l/28interference\)](https://www.openstax.org/l/28interference)

This simulation demonstrates most of the wave phenomena discussed in this section. First, observe interference between two sources of electromagnetic radiation without adding slits. See how water waves, sound, and light all show interference patterns. Stay with light waves and use only one source. Create diffraction patterns with one slit and then with two. You may have to adjust slit width to see the pattern.

Visually compare the slit width to the wavelength. When do you get the best-defined diffraction pattern?

- when the slit width is larger than the wavelength
- when the slit width is smaller than the wavelength
- when the slit width is comparable to the wavelength
- when the slit width is infinite

## Calculations Involving Diffraction and Interference

The fact that the wavelength of light of one color, or **monochromatic** light, can be calculated from its two-slit diffraction pattern in Young's experiments supports the conclusion that light has wave properties. To understand the basis of such calculations, consider how two waves travel from the slits to the screen. Each slit is a different distance from a given point on the screen. Thus different numbers of wavelengths fit into each path. Waves start out from the slits in phase (crest to crest), but they will end up out of phase (crest to trough) at the screen if the paths differ in length by half a wavelength, interfering destructively. If the paths differ by a whole wavelength, then the waves arrive in phase (crest to crest) at the screen, interfering constructively. More generally, if the paths taken by the two waves differ by any half-integral number of wavelengths ( $\frac{1}{2}\lambda$ ,  $\frac{3}{2}\lambda$ ,  $\frac{5}{2}\lambda$ , etc.), then destructive interference occurs. Similarly, if the paths taken by the two waves differ by any integral number of wavelengths ( $\lambda$ ,  $2\lambda$ ,  $3\lambda$ , etc.), then constructive interference occurs.

Figure 17.9 shows how to determine the path-length difference for waves traveling from two slits to a common point on a screen. If the screen is a large distance away compared with the distance between the slits, then the angle  $\theta$  between the path and a line from the slits perpendicular to the screen (see the figure) is nearly the same for each path. That approximation and simple trigonometry show the length difference,  $\Delta L$ , to be  $d \sin \theta$ , where  $d$  is the distance between the slits,

$$\Delta L = d \sin \theta.$$

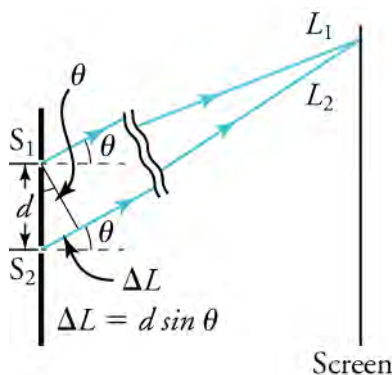
To obtain constructive interference for a double slit, the path-length difference must be an integral multiple of the wavelength, or

$$d \sin \theta = m\lambda, \text{ for } m = 0, 1, -1, 2, -2, \dots \text{ (constructive).}$$

Similarly, to obtain destructive interference for a double slit, the path-length difference must be a half-integral multiple of the wavelength, or

$$d \sin \theta = (m + \frac{1}{2})\lambda, \text{ for } m = 0, 1, -1, 2, -2, \dots \text{ (destructive).}$$

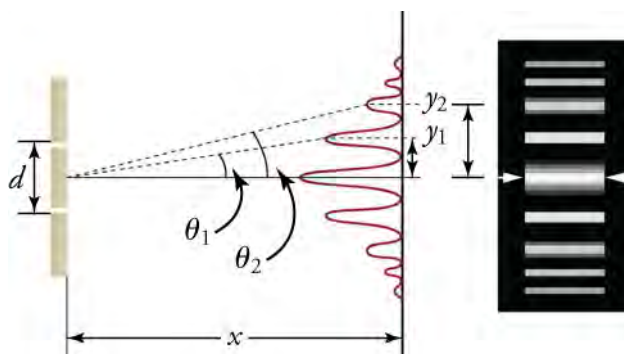
The number  $m$  is the *order* of the interference. For example,  $m = 4$  is fourth-order interference.



**Figure 17.9** The paths from each slit to a common point on the screen differ by an amount  $d \sin \theta$ , assuming the distance to the screen is much greater than the distance between the slits (not to scale here).

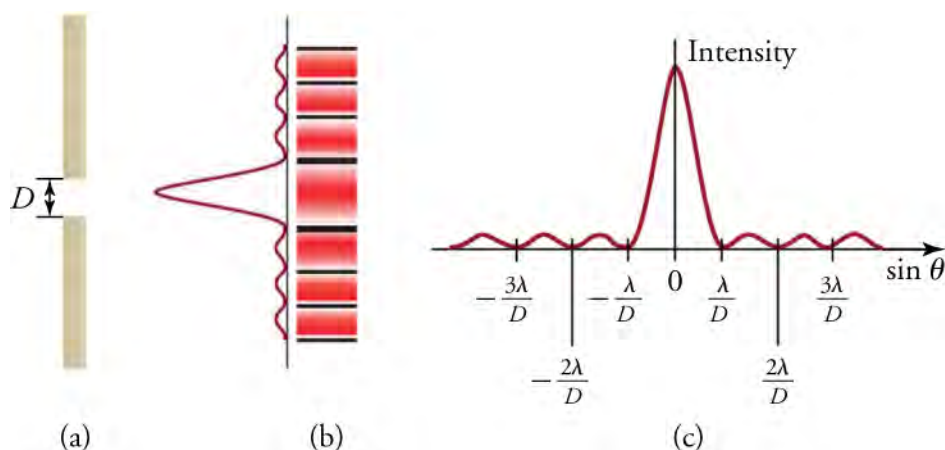
Figure 17.10 shows how the intensity of the bands of constructive interference decreases with increasing angle.





**Figure 17.10** The interference pattern for a double slit has an intensity that falls off with angle. The photograph shows multiple bright and dark lines, or fringes, formed by light passing through a double slit.

Light passing through a single slit forms a diffraction pattern somewhat different from that formed by double slits. [Figure 17.11](#) shows a single-slit diffraction pattern. Note that the central maximum is larger than those on either side, and that the intensity decreases rapidly on either side.



**Figure 17.11** (a) Single-slit diffraction pattern. Monochromatic light passing through a single slit produces a central maximum and many smaller and dimmer maxima on either side. The central maximum is six times higher than shown. (b) The drawing shows the bright central maximum and dimmer and thinner maxima on either side. (c) The location of the minima are shown in terms of  $\lambda$  and  $D$ .

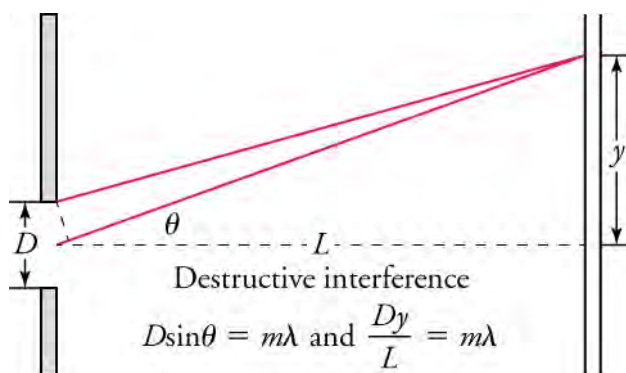
The analysis of single-slit diffraction is illustrated in [Figure 17.12](#). Assuming the screen is very far away compared with the size of the slit, rays heading toward a common destination are nearly parallel. That approximation allows a series of trigonometric operations that result in the equations for the minima produced by destructive interference.

$$D \sin \theta = m\lambda$$

or

$$\frac{Dy}{L} = m\lambda$$

When rays travel straight ahead, they remain in phase and a central maximum is obtained. However, when rays travel at an angle  $\theta$  relative to the original direction of the beam, each ray travels a different distance to the screen, and they can arrive in or out of phase. Thus, a ray from the center travels a distance  $\lambda/2$  farther than the ray from the top edge of the slit, they arrive out of phase, and they interfere destructively. Similarly, for every ray between the top and the center of the slit, there is a ray between the center and the bottom of the slit that travels a distance  $\lambda/2$  farther to the common point on the screen, and so interferes destructively. Symmetrically, there will be another minimum at the same angle below the direct ray.



**Figure 17.12** Equations for a single-slit diffraction pattern, where  $\lambda$  is the wavelength of light,  $D$  is the slit width,  $\theta$  is the angle between a line from the slit to a minimum and a line perpendicular to the screen,  $L$  is the distance from the slit to the screen,  $y$  is the distance from the center of the pattern to the minimum, and  $m$  is a nonzero integer indicating the order of the minimum.

Below we summarize the equations needed for the calculations to follow.

The speed of light in a vacuum,  $c$ , the wavelength of the light,  $\lambda$ , and its frequency,  $f$ , are related as follows.

$$c = f\lambda$$

The wavelength of light in a medium,  $\lambda_n$ , compared to its wavelength in a vacuum,  $\lambda$ , is given by

$$\lambda_n = \frac{\lambda}{n}.$$

17.1

To calculate the positions of constructive interference for a double slit, the path-length difference must be an integral multiple,  $m$ , of the wavelength,  $\lambda$

$$d \sin \theta = m\lambda, \text{ for } m = 0, 1, -1, 2, -2, \dots \text{ (constructive),}$$

where  $d$  is the distance between the slits and  $\theta$  is the angle between a line from the slits to the maximum and a line perpendicular to the barrier in which the slits are located. To calculate the positions of destructive interference for a double slit, the path-length difference must be a half-integral multiple of the wavelength:

$$d \sin \theta = (m + \frac{1}{2})\lambda, \text{ for } m = 0, 1, -1, 2, -2, \dots \text{ (destructive).}$$

For a single-slit diffraction pattern, the width of the slit,  $D$ , the distance of the first ( $m = 1$ ) destructive interference minimum,  $y$ , the distance from the slit to the screen,  $L$ , and the wavelength,  $\lambda$ , are given by

$$\frac{Dy}{L} = \lambda.$$

Also, for single-slit diffraction,

$$D \sin \theta = m\lambda,$$

where  $\theta$  is the angle between a line from the slit to the minimum and a line perpendicular to the screen, and  $m$  is the order of the minimum.



## WORKED EXAMPLE

### Two-Slit Interference

Suppose you pass light from a He-Ne laser through two slits separated by 0.0100 mm, and you find that the third bright line on a screen is formed at an angle of  $10.95^\circ$  relative to the incident beam. What is the wavelength of the light?

#### STRATEGY

The third bright line is due to third-order constructive interference, which means that  $m = 3$ . You are given  $d = 0.0100$  mm and  $\theta = 10.95^\circ$ . The wavelength can thus be found using the equation  $d \sin \theta = m\lambda$  for constructive interference.



**Solution**

The equation is  $d \sin \theta = m\lambda$ . Solving for the wavelength,  $\lambda$ , gives

$$\lambda = \frac{d \sin \theta}{m}.$$

17.2

Substituting known values yields

$$\lambda = \frac{(0.0100 \text{ mm})(\sin 10.95^\circ)}{3} = 6.33 \times 10^{-4} \text{ mm} = 633 \text{ nm}.$$

17.3

**Discussion**

To three digits, 633 nm is the wavelength of light emitted by the common He-Ne laser. Not by coincidence, this red color is similar to that emitted by neon lights. More important, however, is the fact that interference patterns can be used to measure wavelength. Young did that for visible wavelengths. His analytical technique is still widely used to measure electromagnetic spectra. For a given order, the angle for constructive interference increases with  $\lambda$ , so spectra (measurements of intensity versus wavelength) can be obtained.

**WORKED EXAMPLE****Single-Slit Diffraction**

Visible light of wavelength 550 nm falls on a single slit and produces its second diffraction minimum at an angle of  $45.0^\circ$  relative to the incident direction of the light. What is the width of the slit?

**STRATEGY**

From the given information, and assuming the screen is far away from the slit, you can use the equation  $D \sin \theta = m\lambda$  to find  $D$ .

**Solution**

Quantities given are  $\lambda = 550 \text{ nm}$ ,  $m = 2$ , and  $\theta_2 = 45.0^\circ$ . Solving the equation  $D \sin \theta = m\lambda$  for  $D$  and substituting known values gives

$$D = \frac{m\lambda}{\sin \theta} = \frac{2(550 \text{ nm})}{\sin 45.0^\circ} = 1.56 \times 10^{-6} \text{ m}.$$

17.4

**Discussion**

You see that the slit is narrow (it is only a few times greater than the wavelength of light). That is consistent with the fact that light must interact with an object comparable in size to its wavelength in order to exhibit significant wave effects, such as this single-slit diffraction pattern.

**Practice Problems**

1. Monochromatic light from a laser passes through two slits separated by 0.00500 mm. The third bright line on a screen is formed at an angle of  $18.0^\circ$  relative to the incident beam. What is the wavelength of the light?
  - a. 51.5 nm
  - b. 77.3 nm
  - c. 515 nm
  - d. 773 nm
2. What is the width of a single slit through which 610-nm orange light passes to form a first diffraction minimum at an angle of  $30.0^\circ$ ?
  - a. 0.863  $\mu\text{m}$
  - b. 0.704  $\mu\text{m}$
  - c. 0.610  $\mu\text{m}$
  - d. 1.22  $\mu\text{m}$

## Check Your Understanding

- Which aspect of a beam of monochromatic light changes when it passes from a vacuum into water, and how does it change?
  - The wavelength first decreases and then increases.
  - The wavelength first increases and then decreases.
  - The wavelength increases.
  - The wavelength decreases.
- Go outside in the sunlight and observe your shadow. It has fuzzy edges, even if you do not. Is this a diffraction effect? Explain.
  - This is a diffraction effect. Your whole body acts as the origin for a new wavefront.
  - This is a diffraction effect. Every point on the edge of your shadow acts as the origin for a new wavefront.
  - This is a refraction effect. Your whole body acts as the origin for a new wavefront.
  - This is a refraction effect. Every point on the edge of your shadow acts as the origin for a new wavefront.
- Which aspect of monochromatic green light changes when it passes from a vacuum into diamond, and how does it change?
  - The wavelength first decreases and then increases.
  - The wavelength first increases and then decreases.
  - The wavelength increases.
  - The wavelength decreases.

## 17.2 Applications of Diffraction, Interference, and Coherence

### Section Learning Objectives

*By the end of this section, you will be able to do the following:*

- Explain behaviors of waves, including reflection, refraction, diffraction, interference, and coherence, and describe applications based on these behaviors
- Perform calculations related to applications based on wave properties of light

### Section Key Terms

differential interference contrast (DIC)	diffraction grating	iridescence	laser
monochromator	Rayleigh criterion	resolution	

### Wave-Based Applications of Light

In 1917, Albert Einstein was thinking about photons and excited atoms. He considered an atom excited by a certain amount of energy and what would happen if that atom were hit by a photon with the same amount of energy. He suggested that the atom would emit a photon with that amount of energy, and it would be accompanied by the original photon. The exciting part is that you would have *two* photons with the same energy *and* they would be in phase. Those photons could go on to hit other excited atoms, and soon you would have a stream of in-phase photons. Such a light stream is said to be *coherent*. Some four decades later, Einstein's idea found application in a process called, *light amplification by stimulated emission of radiation*. Take the first letters of all the words (except *by* and “of”) and write them in order. You get the word **laser** (see (a)), which is the name of the device that produces such a beam of light.

Laser beams are directional, very intense, and narrow (only about 0.5 mm in diameter). These properties lead to a number of applications in industry and medicine. The following are just a few examples:

- This chapter began with a picture of a compact disc (see ). Those audio and data-storage devices began replacing cassette tapes during the 1990s. CDs are read by interpreting variations in reflections of a laser beam from the surface.
- Some barcode scanners use a laser beam.
- Lasers are used in industry to cut steel and other metals.
- Lasers are bounced off reflectors that astronauts left on the Moon. The time it takes for the light to make the round trip can be used to make precise calculations of the Earth-Moon distance.
- Laser beams are used to produce holograms. The name hologram means *entire picture* (from the Greek *holo-*, as in

*holistic*), because the image is three-dimensional. A viewer can move around the image and see it from different perspectives. Holograms take advantage of the wave properties of light, as opposed to traditional photography which is based on geometric optics. A holographic image is produced by constructive and destructive interference of a split laser beam.

- One of the advantages of using a laser as a surgical tool is that it is accompanied by very little bleeding.
- Laser eye surgery has improved the vision of many people, without the need for corrective lenses. A laser beam is used to change the shape of the lens of the eye, thus changing its focal length.

## Virtual Physics

### Lasers

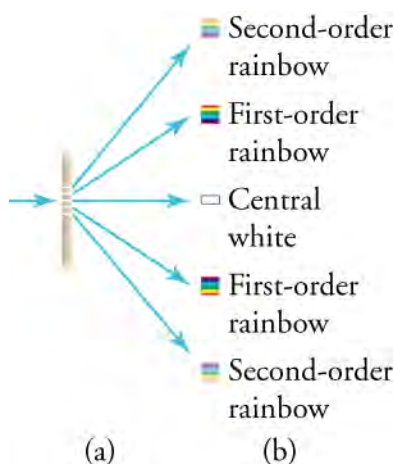
[Click to view content \(https://www.openstax.org/l/28lasers\)](https://www.openstax.org/l/28lasers)

This animation allows you to examine the workings of a laser. First view the picture of a real laser. Change the energy of the incoming photons, and see if you can match it to an excitation level that will produce pairs of coherent photons. Change the excitation level and try to match it to the incoming photon energy.

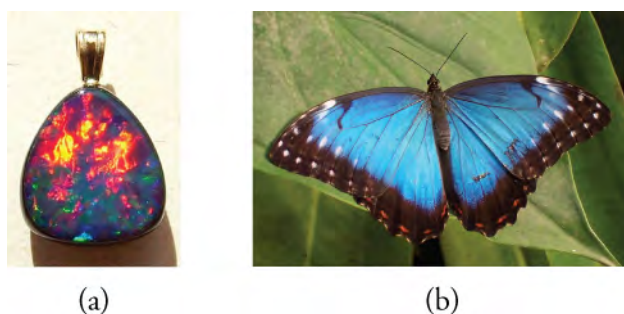
In the animation there is only one excited atom. Is that the case for a real laser? Explain.

- No, a laser would have two excited atoms.
- No, a laser would have several million excited atoms.
- Yes, a laser would have only one excited atom.
- No, a laser would have on the order of  $10^{23}$  excited atoms.

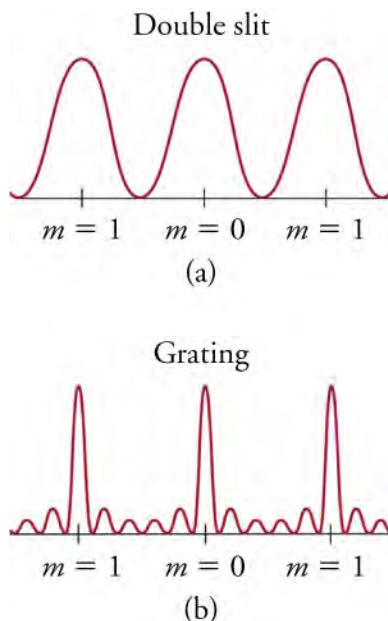
An interesting thing happens if you pass light through a large number of evenly-spaced parallel slits. Such an arrangement of slits is called a **diffraction grating**. An interference pattern is created that is very similar to the one formed by double-slit diffraction (see and ). A diffraction grating can be manufactured by scratching glass with a sharp tool to form a number of precisely positioned parallel lines, which act like slits. Diffraction gratings work both for transmission of light, as in [Figure 17.13](#), and for reflection of light, as on the butterfly wings or the Australian opal shown in [Figure 17.14](#), or the CD pictured in the opening [illustration](#) of this chapter. In addition to their use as novelty items, diffraction gratings are commonly used for spectroscopic dispersion and analysis of light. What makes them particularly useful is the fact that they form a sharper pattern than do double slits. That is, their bright regions are narrower and brighter, while their dark regions are darker. [Figure 17.15](#) shows idealized graphs demonstrating the sharper pattern. Natural diffraction gratings occur in the feathers of certain birds. Tiny, fingerlike structures in regular patterns act as reflection gratings, producing constructive interference that gives the feathers colors not solely due to their pigmentation. The effect is called **iridescence**.



**Figure 17.13** A diffraction grating consists of a large number of evenly-spaced parallel slits. (a) Light passing through the grating is diffracted in a pattern similar to a double slit, with bright regions at various angles. (b) The pattern obtained for white light incident on a grating. The central maximum is white, and the higher-order maxima disperse white light into a rainbow of colors.



**Figure 17.14** (a) This Australian opal and (b) the butterfly wings have rows of reflectors that act like reflection gratings, reflecting different colors at different angles. (credit: (a) Opals-On-Black.com, via Flickr (b) whologwhy, Flickr)



**Figure 17.15** Idealized graphs of the intensity of light passing through a double slit (a) and a diffraction grating (b) for monochromatic light. Maxima can be produced at the same angles, but those for the diffraction grating are narrower, and hence sharper. The maxima become narrower and the regions between become darker as the number of slits is increased.

## Snap Lab

### Diffraction Grating

- A CD (compact disc) or DVD
- A measuring tape
- Sunlight near a white wall

#### Instructions

#### Procedure

1. Hold the CD in direct sunlight near the wall, and move it around until a circular rainbow pattern appears on the wall.
2. Measure the distance from the CD to the wall and the distance from the center of the circular pattern to a color in the rainbow. Use those two distances to calculate  $\tan \theta$ . Find  $\sin \theta$ .
3. Look up the wavelength of the color you chose. That is  $\lambda$ .
4. Solve  $d \sin \theta = m\lambda$  for  $d$ .
5. Compare your answer to the usual spacing between CD tracks, which is 1,600 nm (1.6  $\mu\text{m}$ ).  
How do you know what number to use for  $m$ ?
  - a. Count the rainbow rings preceding the chosen color.

- b. Calculate  $m$  from the frequency of the light of the chosen color.
- c. Calculate  $m$  from the wavelength of the light of the chosen color.
- d. The value of  $m$  is fixed for every color.



## FUN IN PHYSICS

### CD Players

Can you see the grooves on a CD or DVD (see [Figure 17.16](#))? You may think you can because you know they are there, but they are extremely narrow—1,600 in a millimeter. Because the width of the grooves is similar to wavelengths of visible light, they form a diffraction grating. That is why you see rainbows on a CD. The colors are attractive, but they are incidental to the functions of storing and retrieving audio and other data.



**Figure 17.16** For its size, this CD holds a surprising amount of information. Likewise, the CD player it is in houses a surprising number of electronic devices.

The grooves are actually one continuous groove that spirals outward from the center. Data are recorded in the grooves as binary code (zeroes and ones) in small pits. Information in the pits is detected by a laser that tracks along the groove. It gets even more complicated: The speed of rotation must be varied as the laser tracks toward the circumference so that the linear speed along the groove remains constant. There is also an error correction mechanism to prevent the laser beam from getting off track. A diffraction grating is used to create the first two maxima on either side of the track. If those maxima are not the same distance from the track, an error is indicated and then corrected.

The pits are reflective because they have been coated with a thin layer of aluminum. That allows the laser beam to be reflected back and directed toward a photodiode detector. The signal can then be processed and converted to the audio we hear.

The longest wavelength of visible light is about 780 nm. How does that compare to the distance between CD grooves?

- a. The grooves are about 3 times the longest wavelength of visible light.
- b. The grooves are about 2 times the longest wavelength of visible light.
- c. The grooves are about 2 times the shortest wavelength of visible light.
- d. The grooves are about 3 times the shortest wavelength of visible light.



## LINKS TO PHYSICS

### Biology: DIC Microscopy

If you were completely transparent, it would be hard to recognize you from your photograph. The same problem arises when using a traditional microscope to view or photograph small transparent objects such as cells and microbes. Microscopes using **differential interference contrast (DIC)** solve the problem by making it possible to view microscopic objects with enhanced contrast, as shown in [Figure 17.17](#).

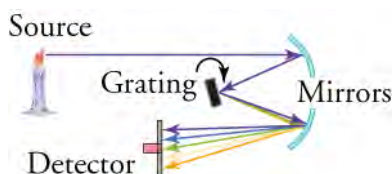


**Figure 17.17** This aquatic organism was photographed with a DIC microscope. (credit: Public Library of Science)

A DIC microscope separates a polarized light source into two beams polarized at right angles to each other and coherent with each other, that is, in phase. After passing through the sample, the beams are recombined and realigned so they have the same plane of polarization. They then create an interference pattern caused by the differences in their optical path and the refractive indices of the parts of the sample they passed through. The result is an image with contrast and shadowing that could not be observed with traditional optics.

Where are diffraction gratings used? Diffraction gratings are key components of **monochromators**—devices that separate the various wavelengths of incoming light and allow a beam with only a specific wavelength to pass through. Monochromators are used, for example, in optical imaging of particular wavelengths from biological or medical samples. A diffraction grating can be chosen to specifically analyze a wavelength of light emitted by molecules in diseased cells in a biopsy sample, or to help excite strategic molecules in the sample with a selected frequency of light. Another important use is in optical fiber technologies where fibers are designed to provide optimum performance at specific wavelengths. A range of diffraction gratings is available for selecting specific wavelengths for such use.

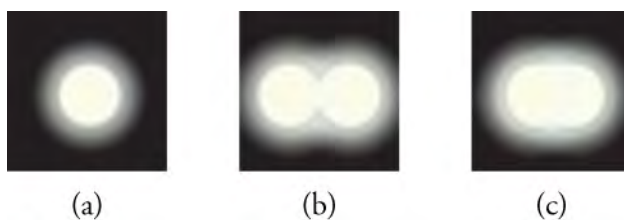
Diffraction gratings are used in spectrosopes to separate a light source into its component wavelengths. When a material is heated to incandescence, it gives off wavelengths of light characteristic of the chemical makeup of the material. A pure substance will produce a spectrum that is unique, thus allowing identification of the substance. Spectrosopes are also used to measure wavelengths both shorter and longer than visible light. Such instruments have become especially useful to astronomers and chemists. [Figure 17.18](#) shows a diagram of a spectrocope.



**Figure 17.18** The diagram shows the function of a diffraction grating in a spectrocope.

Light diffracts as it moves through space, bending around obstacles and interfering constructively and destructively. While diffraction allows light to be used as a spectroscopic tool, it also limits the detail we can obtain in images.

[Figure 17.19](#) (a) shows the effect of passing light through a small circular aperture. Instead of a bright spot with sharp edges, a spot with a fuzzy edge surrounded by circles of light is obtained. This pattern is caused by diffraction similar to that produced by a single slit. Light from different parts of the circular aperture interferes constructively and destructively. The effect is most noticeable when the aperture is small, but the effect is there for large apertures, too.



**Figure 17.19** (a) Monochromatic light passed through a small circular aperture produces this diffraction pattern. (b) Two point light sources that are close to one another produce overlapping images because of diffraction. (c) If they are closer together, they cannot be resolved, that is, distinguished.

How does diffraction affect the detail that can be observed when light passes through an aperture? [Figure 17.19](#) (b) shows the diffraction pattern produced by two point light sources that are close to one another. The pattern is similar to that for a single point source, and it is just barely possible to tell that there are two light sources rather than one. If they are closer together, as in [Figure 17.19](#) (c), you cannot distinguish them, thus limiting the detail, or **resolution**, you can obtain. That limit is an inescapable consequence of the wave nature of light.

There are many situations in which diffraction limits the resolution. The acuity of vision is limited because light passes through the pupil, the circular aperture of the eye. Be aware that the diffraction-like spreading of light is due to the limited diameter of a light beam, not the interaction with an aperture. Thus light passing through a lens with a diameter of  $D$  shows the diffraction effect and spreads, blurring the image, just as light passing through an aperture of diameter  $D$  does. Diffraction limits the resolution of any system having a lens or mirror. Telescopes are also limited by diffraction, because of the finite diameter,  $D$ , of their primary mirror.

Why are diffraction gratings used in spectroscopes rather than just two slits?

- The bands produced by diffraction gratings are dimmer but sharper than the bands produced by two slits.
- The bands produced by diffraction gratings are brighter, though less sharp, than the bands produced by two slits.
- The bands produced by diffraction gratings are brighter and sharper than the bands produced by two slits.
- The bands produced by diffraction gratings are dimmer and less sharp, but more widely dispersed, than the bands produced by two slits.

## Calculations Involving Diffraction Gratings and Resolution

Early in the chapter, it was mentioned that when light passes from one medium to another, its speed and wavelength change, but its frequency remains constant. The equation

$$\lambda_n = \frac{\lambda}{n}$$

shows how the wavelength in a given medium,  $\lambda_n$ , is related to the wavelength in a vacuum,  $\lambda$ , and the refractive index,  $n$ , of the medium. The equation is useful for calculating the change in wavelength of a monochromatic laser beam in various media. The analysis of a diffraction grating is very similar to that for a double slit. As you know from the discussion of double slits in Young's double-slit experiment, light is diffracted by, and spreads out after passing through, each slit. Rays travel at an angle  $\theta$  relative to the incident direction. Each ray travels a different distance to a common point on a screen far away. The rays start in phase, and they can be in or out of phase when they reach a screen, depending on the difference in the path lengths traveled. Each ray travels a distance that differs by  $d \sin \theta$  from that of its neighbor, where  $d$  is the distance between slits. If  $d \sin \theta$  equals an integral number of wavelengths, the rays all arrive in phase, and constructive interference (a maximum) is obtained. Thus, the condition necessary to obtain constructive interference for a diffraction grating is

$$d \sin \theta = m\lambda, \text{ for } m = 0, 1, -1, 2, -2, \dots,$$

where  $d$  is the distance between slits in the grating,  $\lambda$  is the wavelength of the light, and  $m$  is the order of the maximum. Note that this is exactly the same equation as for two slits separated by  $d$ . However, the slits are usually closer in diffraction gratings than in double slits, producing fewer maxima at larger angles.





## WATCH PHYSICS

### Diffraction Grating

This [video \(https://www.openstax.org/l/28diffraction\)](https://www.openstax.org/l/28diffraction) explains the geometry behind the diffraction pattern produced by a diffraction grating.

[Click to view content \(https://www.openstax.org/l/28diffraction\)](https://www.openstax.org/l/28diffraction)

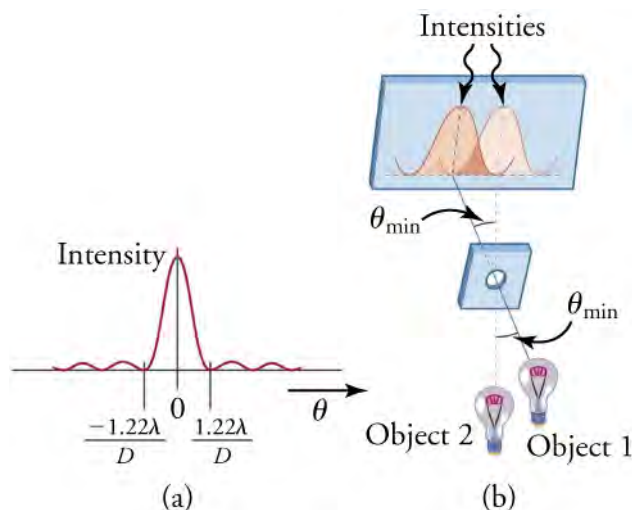
The equation that gives the points of constructive interference produced by a diffraction grating is  $d \sin \theta = m\lambda$ . Why does that equation look familiar?

- It is the same as the equation for destructive interference for a double-slit diffraction pattern.
- It is the same as the equation for constructive interference for a double-slit diffraction pattern.
- It is the same as the equation for constructive interference for a single-slit diffraction pattern.
- It is the same as the equation for destructive interference for a single-slit diffraction pattern.

Just what is the resolution limit of an aperture or lens? To answer that question, consider the diffraction pattern for a circular aperture, which, similar to the diffraction pattern of light passing through a slit, has a central maximum that is wider and brighter than the maxima surrounding it (see [Figure 17.19](#) (a)). It can be shown that, for a circular aperture of diameter  $D$ , the first minimum in the diffraction pattern occurs at  $\theta = 1.22\lambda/D$ , provided that the aperture is large compared with the wavelength of light, which is the case for most optical instruments. The accepted criterion for determining the diffraction limit to resolution based on diffraction was developed by Lord Rayleigh in the 19th century. The **Rayleigh criterion** for the diffraction limit to resolution states that two images are just resolvable when the center of the diffraction pattern of one is directly over the first minimum of the diffraction pattern of the other. See [Figure 17.20](#) (b). The first minimum is at an angle of  $\theta = 1.22\lambda/D$ , so that two point objects are just resolvable if they are separated by the angle

$$\theta = 1.22 \frac{\lambda}{D},$$

where  $\lambda$  is the wavelength of the light (or other electromagnetic radiation) and  $D$  is the diameter of the aperture, lens, mirror, etc., with which the two objects are observed. In the expression above,  $\theta$  has units of radians.



**Figure 17.20** (a) Graph of intensity of the diffraction pattern for a circular aperture. Note that, similar to a single slit, the central maximum is wider and brighter than those to the sides. (b) Two point objects produce overlapping diffraction patterns. Shown here is the Rayleigh criterion for their being just resolvable. The central maximum of one pattern lies on the first minimum of the other.

## Snap Lab

### Resolution

- A sheet of white paper
- A black pen or pencil
- A measuring tape

#### Instructions

#### Procedure

1. Draw two lines several mm apart on a white sheet of paper.
2. Move away from the sheet as it is held upright, and measure the distance at which you can just distinguish (resolve) the lines as separate.
3. Use  $\theta = 1.22 \frac{\lambda}{D}$  to calculate  $D$  the diameter of your pupil. Use the distance between the lines and the maximum distance at which they were resolved to calculate  $\theta$ . Use the average wavelength for visible light as the value for  $\lambda$ .
4. Compare your answer to the average pupil diameter of 3 mm.

Describe resolution in terms of minima and maxima of diffraction patterns.

- a. The limit for resolution is when the minimum of the pattern for one of the lines is directly over the first minimum of the pattern for the other line.
- b. The limit for resolution is when the maximum of the pattern for one of the lines is directly over the first minimum of the pattern for the other line.
- c. The limit for resolution is when the maximum of the pattern for one of the lines is directly over the second minimum of the pattern for the other line.
- d. The limit for resolution is when the minimum of the pattern for one of the lines is directly over the second maximum of the pattern for the other line.



## WORKED EXAMPLE

### Change of Wavelength

A monochromatic laser beam of green light with a wavelength of 550 nm passes from air to water. The refractive index of water is 1.33. What will be the wavelength of the light after it enters the water?

#### STRATEGY

You can assume that the refractive index of air is the same as that of light in a vacuum because they are so close. You then have all the information you need to solve for  $\lambda_n$ .

#### Solution

$$\lambda_n = \frac{\lambda}{n} = \frac{550 \text{ nm}}{1.33} = 414 \text{ nm}$$

17.5

#### Discussion

The refractive index of air is 1.0003, so the approximation holds for three significant figures. You would not see the light change color, however. Color is determined by frequency, not wavelength.



## WORKED EXAMPLE

### Diffraction Grating

A diffraction grating has 2000 lines per centimeter. At what angle will the first-order maximum form for green light with a wavelength of 520 nm?

#### STRATEGY

You are given enough information to calculate  $d$ , and you are given the values of  $\lambda$  and  $m$ . You will have to find the arcsin of a

number to find  $\theta$ .

### Solution

First find  $d$ .

$$d = \frac{1 \text{ cm}}{2,000} = 5.00 \times 10^{-4} \text{ cm} = 5,000 \text{ nm}$$

17.6

Rearrange the equation for constructive interference conditions for a diffraction grating, and substitute the known values.

$$\begin{aligned} d \sin \theta &= m\lambda \\ \theta &= \sin^{-1} \frac{m\lambda}{d} \\ &= \sin^{-1} \left( \frac{(1)(520)}{5,000} \right) \\ &= 5.97 \end{aligned}$$

### Discussion

This angle seems reasonable for the first maximum. Recall that the meaning of  $\sin^{-1}$  (or arcsin) is *the angle with a sine that is (the unknown)*. Remember that the value of  $\sin \theta$  will not be greater than 1 for any value of  $\theta$ .



## WORKED EXAMPLE

### Resolution

What is the minimum angular spread of a 633-nm-wavelength He-Ne laser beam that is originally 1.00 mm in diameter?

#### STRATEGY

The diameter of the beam is the same as if it were coming through an aperture of that size, so  $D = 1.00$  mm. You are given  $\lambda$ , and you must solve for  $\theta$ .

#### Solution

$$\theta = \frac{(1.22)\lambda}{D} = \frac{(1.22)(633 \text{ nm})}{1.00 \times 10^6 \text{ nm}} = 7.72 \times 10^{-4} \text{ rad} = 0.0442^\circ$$

17.7

### Discussion

The conversion factor for radians to degrees is  $1.000 \text{ radian} = 57.3^\circ$ . The spread is very small and would not be noticeable over short distances. The angle represents the angular separation of the central maximum and the first minimum.

## Practice Problems

- A beam of yellow light has a wavelength of 600 nm in a vacuum and a wavelength of 397 nm in Plexiglas. What is the refractive index of Plexiglas?
  - 1.51
  - 2.61
  - 3.02
  - 3.77
- What is the angle between two just-resolved points of light for a 3.00 mm diameter pupil, assuming an average wavelength of 550 nm?
  - 224 rad
  - 183 rad
  - $1.83 \times 10^{-4}$  rad
  - $2.24 \times 10^{-4}$  rad

## Check Your Understanding

- How is an interference pattern formed by a diffraction grating different from the pattern formed by a double slit?

- a. The pattern is colorful.
  - b. The pattern is faded.
  - c. The pattern is sharper.
  - d. The pattern is curved.
9. A beam of light always spreads out. Why can a beam not be produced with parallel rays to prevent spreading?
- a. Light is always polarized.
  - b. Light is always reflected.
  - c. Light is always refracted.
  - d. Light is always diffracted.
10. Compare interference patterns formed by a double slit and by a diffraction grating in terms of brightness and narrowness of bands.
- a. The pattern formed has broader and brighter bands.
  - b. The pattern formed has broader and duller bands.
  - c. The pattern formed has narrower and duller bands.
  - d. The pattern formed has narrower and brighter bands.
11. Describe the slits in a diffraction grating in terms of number and spacing, as compared to a two-slit diffraction setup.
- a. The slits in a diffraction grating are broader, with space between them that is greater than the separation of the two slits in two-slit diffraction.
  - b. The slits in a diffraction grating are broader, with space between them that is the same as the separation of the two slits in two-slit diffraction.
  - c. The slits in a diffraction grating are narrower, with space between them that is the same as the separation of the two slits in two-slit diffraction.
  - d. The slits in a diffraction grating are narrower, with space between them that is greater than the separation of the two slits in two-slit diffraction.

## KEY TERMS

**differential interference contrast (DIC)** separating a polarized light source into two beams polarized at right angles to each other and coherent with each other then, after passing through the sample, recombining and realigning the beams so they have the same plane of polarization, and then creating an interference pattern caused by the differences in their optical path and the refractive indices of the parts of the sample they passed through; the result is an image with contrast and shadowing that could not be observed with traditional optics

**diffraction** bending of a wave around the edges of an opening or an obstacle

**diffraction grating** many of evenly spaced slits having dimensions such that they produce an interference pattern

**Huygens's principle** Every point on a wavefront is a source of wavelets that spread out in the forward direction at the same speed as the wave itself; the new wavefront is a line

tangent to all of the wavelets.

**iridescence** the effect that occurs when tiny, fingerlike structures in regular patterns act as reflection gratings, producing constructive interference that gives feathers colors not solely due to their pigmentation

**laser** acronym for a device that produces *light amplification by stimulated emission of radiation*

**monochromatic** one color

**monochromator** device that separates the various wavelengths of incoming light and allows a beam with only a specific wavelength to pass through

**Rayleigh criterion** two images are just resolvable when the center of the diffraction pattern of one is directly over the first minimum of the diffraction pattern of the other

**resolution** degree to which two images can be distinguished from one another, which is limited by diffraction

**wavefront** points on a wave surface that all share an identical, constant phase

## SECTION SUMMARY

### 17.1 Understanding Diffraction and Interference

- The wavelength of light varies with the refractive index of the medium.
- Slits produce a diffraction pattern if their width and separation are similar to the wavelength of light passing through them.
- Interference bands of a single-slit diffraction pattern can be predicted.
- Interference bands of a double-slit diffraction pattern can be predicted.

### 17.2 Applications of Diffraction, Interference, and Coherence

- The focused, coherent radiation emitted by lasers has many uses in medicine and industry.
- Characteristics of diffraction patterns produced with diffraction gratings can be determined.
- Diffraction gratings have been incorporated in many instruments, including microscopes and spectrometers.
- Resolution has a limit that can be predicted.

## KEY EQUATIONS

### 17.1 Understanding Diffraction and Interference

speed of light, frequency, and wavelength  $c = f\lambda$

change of wavelength with index of refraction  $\lambda_n = \frac{\lambda}{n}$

two-slit constructive interference  $d \sin \theta = m\lambda$ , for  $m = 0, 1, -1, 2, -2, \dots$

two-slit destructive interference  $d \sin \theta = (m + \frac{1}{2})\lambda$ , for  $m = 0, 1, -1, 2, -2, \dots$

one-slit, first-order destructive interference; wavelength related to dimensions  $\frac{Dy}{L} = \lambda$

one-slit destructive interference  $D \sin \theta = m\lambda$

## 17.2 Applications of Diffraction, Interference, and Coherence

wavelength change with change in medium

$$\lambda_n = \frac{\lambda}{n}$$

diffraction grating constructive interference

$$d \sin \theta = m\lambda$$

resolution

$$\theta = 1.22 \frac{\lambda}{D}$$

## CHAPTER REVIEW

### Concept Items

#### 17.1 Understanding Diffraction and Interference

- Which behavior of light is indicated by an interference pattern?
  - ray behavior
  - particle behavior
  - corpuscular behavior
  - wave behavior
- Which behavior of light is indicated by diffraction?
  - wave behavior
  - particle behavior
  - ray behavior
  - corpuscular behavior

#### 17.2 Applications of Diffraction, Interference, and Coherence

- There is a principle related to resolution that is expressed by this equation.

$$\theta = \frac{\lambda}{D}$$

17.8

What is that principle stated in full?

### Critical Thinking Items

#### 17.1 Understanding Diffraction and Interference

- Describe a situation in which bodies of water and a line of rocks could create a diffraction pattern similar to light passing through double slits. Include the arrangement of the rocks, the positions of the bodies of water, and the location of the diffraction pattern. Note the dimensions that are necessary for the production of the pattern.
  - When waves from a small body of water pass through two widely separated openings and enter a larger body of water, a diffraction pattern is produced that is similar to the diffraction pattern formed by light passing through two slits. The width of each opening is larger than the size of the wavelength of the waves.
  - When waves from a large body of water pass

- A principle related to resolution states, "Two images are just resolved when the center of the diffraction pattern of one is directly over the first minimum of the diffraction pattern of the other." Write the equation that expresses that principle.
  - $\theta = 1.22 \frac{D}{\lambda}$
  - $\theta = \frac{D}{\lambda}$
  - $\theta = \frac{\lambda}{D}$
  - $\theta = 1.22 \frac{\lambda}{D}$
- Which statement completes this resolution? Two images are just resolved when —
  - The center of the diffraction pattern of one image is directly over the central maximum of the diffraction pattern of the other.
  - The center of the diffraction pattern of one image is directly over the central minimum of the diffraction pattern of the other.
  - The center of the diffraction pattern of one image is directly over the first minimum of the diffraction pattern of the other.
  - The center of the diffraction pattern of one is directly over the first maximum of the diffraction pattern of the other.

through two narrow openings and enter a smaller body of water, a diffraction pattern is produced that is similar to the diffraction pattern formed by light passing through two slits. The widths and separation of the openings are similar to the size of the wavelength of the waves.

- When waves from a small body of water pass through two wide openings and enter a larger body of water, a diffraction pattern is produced that is similar to the diffraction pattern formed by light passing through two slits. The separation between the openings is similar to the size of the wavelength of the waves.
- When waves from a large body of water pass through two wide openings and enter a smaller body of water, a diffraction pattern is produced that is similar to the diffraction pattern formed by light passing through two slits. The widths and

separation of the openings are larger than the size of the wavelength of the waves.

## 17.2 Applications of Diffraction, Interference, and Coherence

7. For what type of electromagnetic radiation would a grating with spacing greater than 800 nm be useful as a spectroscopic tool?
  - a. It can be used to analyze spectra only in the infrared portion of the spectrum.
  - b. It can be used to analyze spectra in the entire visible portion of the electromagnetic spectrum.

- c. It can only be used to analyze spectra in the short-wavelength visible.
- d. It can only be used to analyze spectra in the short-wavelength visible and ultraviolet.

8. A beam of green light has a wavelength of 500 nm in a vacuum and a wavelength of 331 nm in Plexiglas. What is the refractive index of Plexiglas?
  - a. 1.12
  - b. 1.25
  - c. 1.51
  - d. 4.53

## Problems

### 17.1 Understanding Diffraction and Interference

9. What is the distance between two slits that produce a diffraction pattern with the first minimum at an angle of  $45.0^\circ$  when 410-nm violet light passes through the slits?
  - a. 2,030 nm
  - b. 1,450 nm
  - c. 410 nm
  - d. 290 nm
10. A breakwater at the entrance to a harbor consists of a rock barrier with a 50.0-m-wide opening. Ocean waves with a 20.0-m wavelength approach the opening straight on. At what angle to the incident direction are the boats inside the harbor most protected against wave action?
  - a.  $11.5^\circ$
  - b.  $7.46^\circ$
  - c.  $5.74^\circ$
  - d.  $23.6^\circ$

### 17.2 Applications of Diffraction, Interference, and Coherence

11. A 500-nm beam of light passing through a diffraction grating creates its second band of constructive interference at an angle of  $1.50^\circ$ . How far apart are the slits in the grating?
  - a. 38,200 nm
  - b. 19,100 nm
  - c. 667 nm
  - d. 333 nm
12. The range of the visible-light spectrum is 380 nm to 780 nm. What is the maximum number of lines per centimeter a diffraction grating can have and produce a complete first-order spectrum for visible light?
  - a. 26,300 lines/cm
  - b. 13,200 lines/cm
  - c. 6,410 lines/cm
  - d. 12,820 lines/cm

## Performance Task

### 17.2 Applications of Diffraction, Interference, and Coherence

13. In this performance task you will create one- and two-slit diffraction and observe the interference patterns that result.
  - A utility knife (a knife with a razor blade-like cutting edge)
  - Aluminum foil
  - A straight edge
  - A strong, small light source or a laser pointer
  - A tape measure
  - A white wall

## Procedure

1. Cut a piece of aluminum foil about 15 cm  $\times$  15 cm.
2. Use the utility knife and the straight edge to cut a straight slit several cm long in the center of the foil square.
3. With the room darkened, one partner shines the light through the slit and toward the wall. The other partner observes the pattern on the wall. The partner with the light changes the distance from the foil to the wall and the distance from the light to the foil.
4. When the sharpest, brightest pattern possible is obtained, the partner who is not holding the foil and light makes measurements.
5. Measure the perpendicular (shortest) distance from



the slit to the wall, the distance from the center of the pattern to several of the dark bands, and the distance from the slit to the same dark bands.

6. Carefully make a second slit parallel to the first slit and 1 mm or less away.
7. Repeat steps 2 through 5, only this time measure the distances to bright bands.

NOTE—In your calculations, use 580 nm for  $\lambda$  if you used white light. If you used a colored laser pointer, look up the wavelength of the color. You may find it easier to calculate  $\theta$  from its tangent

rather than from its sine.

- a. Which experiment gave the most distinct pattern—one or two slits?
- b. What was the width of the single slit? Compare the calculated distance with the measured distance.
- c. What was the distance between the two slits? Compare the calculated distance with the measured distance.

## TEST PREP

### Multiple Choice

#### 17.1 Understanding Diffraction and Interference

14. Which remains unchanged when a monochromatic beam of light passes from air into water?
  - a. the speed of the light
  - b. the direction of the beam
  - c. the frequency of the light
  - d. the wavelength of the light
15. Two slits are separated by a distance of 3500 nm. If light with a wavelength of 500 nm passes through the slits and produces an interference pattern, the  $m = \underline{\hspace{1cm}}$  order minimum appears at an angle of  $30.0^\circ$ .
  - a. 0
  - b. 1
  - c. 2
  - d. 3
16. In the sunlight, the shadow of a building has fuzzy edges even if the building does not. Is this a refraction effect? Explain.
  - a. Yes, this is a refraction effect, where every point on the building acts as the origin for a new wavefront.
  - b. Yes, this is a refraction effect, where the whole building acts as the origin for a new wavefront.
  - c. No, this is a diffraction effect, where every point on the edge of the building's shadow acts as the origin for a new wavefront.
  - d. No, this is a diffraction effect, where the whole building acts as the origin for a new wavefront.

#### 17.2 Applications of Diffraction, Interference, and Coherence

17. Two images are just resolved when the center of the diffraction pattern of one is directly over          of the diffraction pattern of the other.
  - a. the center

- b. the first minimum
- c. the first maximum
- d. the last maximum

18. Two point sources of 500 nm light are just resolvable as they pass through a small hole. The angle to the first minimum of one source is  $0.100$  rad. What is the diameter of the hole?
  - a.  $4.10 \mu\text{m}$
  - b.  $5.73 \mu\text{m}$
  - c.  $0.106 \mu\text{m}$
  - d.  $6.10 \mu\text{m}$
19. Will a beam of light shining through a 1-mm hole behave any differently than a beam of light that is 1 mm wide as it leaves its source? Explain.
  - a. Yes, the beam passing through the hole will spread out as it travels, because it is diffracted by the edges of the hole, whereas the 1-mm beam, which encounters no diffracting obstacle, will not spread out.
  - b. Yes, the beam passing through the hole will be made *more parallel* by passing through the hole, and so will not spread out as it travels, whereas the unaltered wavefronts of the 1-mm beam will cause the beam to spread out as it travels.
  - c. No, both beams will remain the same width as they travel, and they will not spread out.
  - d. No, both beams will spread out as they travel.
20. A laser pointer emits a coherent beam of parallel light rays. Does the light from such a source spread out at all? Explain.
  - a. Yes, every point on a wavefront is not a source of wavelets, which prevent the spreading of light waves.
  - b. No, every point on a wavefront is not a source of wavelets, so that the beam behaves as a bundles of rays that travel in their initial direction.
  - c. No, every point on a wavefront is a source of

- wavelets, which keep the beam from spreading.
- d. Yes, every point on a wavefront is a source of

wavelets, which cause the beam to spread out steadily as it moves forward.

## Short Answer

### 17.1 Understanding Diffraction and Interference

21. Light passing through double slits creates a diffraction pattern. How would the spacing of the bands in the pattern change if the slits were closer together?
- The bands would be closer together.
  - The bands would spread farther apart.
  - The bands would remain stationary.
  - The bands would fade and eventually disappear.
22. A beam of light passes through a single slit to create a diffraction pattern. How will the spacing of the bands in the pattern change if the width of the slit is increased?
- The width of the spaces between the bands will remain the same.
  - The width of the spaces between the bands will increase.
  - The width of the spaces between the bands will decrease.
  - The width of the spaces between the bands will first decrease and then increase.
23. What is the wavelength of light falling on double slits separated by  $2.00\ \mu\text{m}$  if the third-order maximum is at an angle of  $60.0^\circ$ ?
- 667 nm
  - 471 nm
  - 333 nm
  - 577 nm
24. What is the longest wavelength of light passing through a single slit of width  $1.20\ \mu\text{m}$  for which there is a first-order minimum?
- $1.04\ \mu\text{m}$
  - $0.849\ \mu\text{m}$
  - $0.600\ \mu\text{m}$
  - $2.40\ \mu\text{m}$

### 17.2 Applications of Diffraction, Interference, and Coherence

25. Describe a diffraction grating and the interference pattern it produces.
- A diffraction grating is a large collection of evenly

spaced parallel lines that produces an interference pattern that is similar to but sharper and better dispersed than that of a double slit.

- A diffraction grating is a large collection of randomly spaced parallel lines that produces an interference pattern that is similar to but less sharp or well-dispersed as that of a double slit.
  - A diffraction grating is a large collection of randomly spaced intersecting lines that produces an interference pattern that is similar to but sharper and better dispersed than that of a double slit.
  - A diffraction grating is a large collection of evenly spaced intersecting lines that produces an interference pattern that is similar to but less sharp or well-dispersed as that of a double slit.
26. Suppose pure-wavelength light falls on a diffraction grating. What happens to the interference pattern if the same light falls on a grating that has more lines per centimeter?
- The bands will spread farther from the central maximum.
  - The bands will come closer to the central maximum.
  - The bands will not spread farther from the first maximum.
  - The bands will come closer to the first maximum.
27. How many lines per centimeter are there on a diffraction grating that gives a first-order maximum for 473 nm blue light at an angle of  $25.0^\circ$ ?
- 529,000 lines/cm
  - 50,000 lines/cm
  - 851 lines/cm
  - 8,934 lines/cm
28. What is the distance between lines on a diffraction grating that produces a second-order maximum for 760-nm red light at an angle of  $60.0^\circ$ ?
- $2.28 \times 10^4\ \text{nm}$
  - $3.29 \times 10^2\ \text{nm}$
  - $2.53 \times 10^1\ \text{nm}$
  - $1.76 \times 10^3\ \text{nm}$

## Extended Response

### 17.1 Understanding Diffraction and Interference

29. Suppose you use a double slit to perform Young's double-slit experiment in air, and then repeat the experiment with the same double slit in water. Does the color of the light change? Do the angles to the same parts of the interference pattern get larger or smaller? Explain.
- No, the color is determined by frequency. The magnitude of the angle decreases.
  - No, the color is determined by wavelength. The magnitude of the angle decreases.
  - Yes, the color is determined by frequency. The magnitude of the angle increases.
  - Yes, the color is determined by wavelength. The magnitude of the angle increases.
30. A double slit is located at a distance  $x$  from a screen, with the distance along the screen from the center given by  $y$ . When the distance  $d$  between the slits is relatively large, there will be numerous bright bands. For small angles (where  $\sin\theta = \theta$ , with  $\theta$  in radians), what is the distance between fringes?
- $\Delta y = \frac{d}{x\lambda}$
  - $\Delta y = \frac{x\lambda}{d}$
  - $\Delta y = \frac{\lambda}{xd}$
  - $\Delta y = \frac{x\lambda}{d}$

### 17.2 Applications of Diffraction, Interference, and Coherence

31. Compare the interference patterns of single-slit diffraction, double-slit diffraction, and a diffraction

grating.

- All three interference pattern produce identical bands.
  - A double slit produces the sharpest and most distinct bands.
  - A single slit produces the sharpest and most distinct bands.
  - The diffraction grating produces the sharpest and most distinct bands.
32. An electric current through hydrogen gas produces several distinct wavelengths of visible light. The light is projected onto a diffraction grating having 10,000 lines per centimeter. What are the wavelengths of the hydrogen spectrum if the light forms first-order maxima at angles of  $24.2^\circ$ ,  $25.7^\circ$ ,  $29.1^\circ$ , and  $41.0^\circ$ ?
- $\lambda_1 = (10^3 \text{ nm}) \sin 24.2^\circ = 410 \text{ nm}$   
 $\lambda_2 = (10^3 \text{ nm}) \sin 25.7^\circ = 434 \text{ nm}$   
 $\lambda_3 = (10^3 \text{ nm}) \sin 29.1^\circ = 486 \text{ nm}$   
 $\lambda_4 = (10^3 \text{ nm}) \sin 41.0^\circ = 656 \text{ nm}$
  - $\lambda_1 = (10^3 \text{ nm}) \sin 41.0^\circ = 410 \text{ nm}$   
 $\lambda_2 = (10^3 \text{ nm}) \sin 25.7^\circ = 434 \text{ nm}$   
 $\lambda_3 = (10^3 \text{ nm}) \sin 29.1^\circ = 486 \text{ nm}$   
 $\lambda_4 = (10^3 \text{ nm}) \sin 24.2^\circ = 656 \text{ nm}$
  - $\lambda_1 = (10^3 \text{ nm}) \sin 24.2^\circ = 410 \text{ nm}$   
 $\lambda_2 = (10^3 \text{ nm}) \sin 29.1^\circ = 434 \text{ nm}$   
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 $\lambda_3 = (10^3 \text{ nm}) \sin 25.7^\circ = 486 \text{ nm}$   
 $\lambda_4 = (10^3 \text{ nm}) \sin 24.2^\circ = 656 \text{ nm}$

